

## Comparing the HT estimator and the ratio estimator

Here is some R code that should help you do HW assignment 6. You should read the details of assignment 6 in the syllabus carefully before looking at this code.

The only code you will have to change is the last few lines after the line `set.seed(2004)`. Of course you will have to consider various designs. It will probably be helpful to look at other functions of `popx` as possible designs.

```
> getans<-function(est,stderr,truetot)
+ {
+   err<-abs(est-truetot)
+   lwbd<-est -1.96*stderr
+   upbd<-est + 1.96*stderr
+   if(lwbd <= truetot & truetot <= upbd) { cov<-1}
+   else {cov<-0}
+   ans<-c(est,err,lwbd,upbd - lwbd,cov)
+   return(ans)
+ }
> srstot<-function(smp,popy)
+ {
+   n<-length(smp)
+   N<-length(popy)
+   fpc<-1-n/N
+   ysmp<-popy[smp]
+   est<-N*mean(ysmp)
+   stderr<-N*sqrt((fpc/n)*var(ysmp))
+   ans<-getans(est,stderr,sum(popy))
+   return(ans)
+ }
> ratiotot<-function(smp,popy,popx)
+ {
+   n <- length(smp)
+   N<-length(popx)
+   ff<-n/N
+   ysamp<-popy[smp]
+   xsamp<-popx[smp]
+   tx<-sum(popx)
+   trtot<-sum(popy)
+   rhat <- sum(ysamp)/sum(xsamp)
+   est <- rhat * tx
+   dum1<-(N*N*(1-ff))/(n*(n-1))
+   vartot <- dum1*sum((ysamp-rhat*xsamp)^2)
+   stderr<-sqrt(vartot)
+   ans<-getans(est,stderr,sum(popy))
+   return(ans)
+ }
```

```

+ }
> httot<-function(smp,popy,designwts)
+ {
+   wts<-designwts[smp]
+   est<-sum(wts*popy[smp])
+   n<-length(smp)
+   dum<-sum((n*wts*popy[smp] - est)^2)
+   stderr<-sqrt((1/(n*(n-1))*dum))
+   ans<-getans(est,stderr,sum(popy))
+   return(ans)
+ }
> compar3est<-function(popy,popx,design,n)
+ {
+   designwts<-sum(design)/(n*design)
+   smp<-sample(1:length(popy),n,replace=FALSE,prob=design)
+   ansrs<-srstot(smp,popy)
+   ansHT<-httot(smp,popy,designwts)
+   ansratio<-ratiotot(smp,popy,popx)
+   ans<-rbind(ansrs,ansHT,ansratio)
+   return(ans)
+ }
> compar3estlp<-function(popy,popx,design,n,R)
+ {
+   ans<-matrix(0,3,5)
+   for(i in 1:R){
+     ans<-ans + compar3est(popy,popx,design,n)
+   }
+   ans<-round(ans/R,digits=3)
+   return(ans)
+ }
> set.seed(2004)
> popx<-rlnorm(500,10,.4)
> popy<-rnorm(500,0.1*popx,3*sqrt(popx))
> sum(popy)

[1] 1232136

> cor(popx,popy)

[1] 0.9203

> n<-50
> R<-500
> design<-popx
> compar3estlp(popy,popx,design,n,R)

      [,1]      [,2]      [,3]      [,4]      [,5]
ansrs 1439359 207313.61 1268065 342586.8 0.328

```

```
ansHT      1232135  24660.52 1168937 126397.3 0.966
ansratio 1239790  22754.39 1176851 125878.2 0.970
```

```
> design<-rep(1,length(popy))
> compar3estlp(popy,popx,design,n,R)
```

```
          [,1]      [,2]      [,3]      [,4]      [,5]
anssrs 1234516 63158.28 1083825 301382.6 0.942
ansHT   1234516 63158.28 1075674 317685.1 0.952
ansratio 1232362 24560.78 1172819 119085.1 0.946
```