## Stat 5101 (Geyer) Fall 2014 Homework Assignment 1 Due Wednesday, September 10, 2014

Solve each problem. Explain your reasoning. No credit for answers with no explanation.

**1-1.** For each of the following functions h either determine a constant c such that  $c \cdot h$  — that is, the function  $x \mapsto c \cdot h(x)$  — is a PMF or determine that no such constant exists.

- (a) the identity function on the set  $\{0, 1, 2\}$ .
- (b) the identity function on the set  $\{-2, -1, 0, 1, 2\}$ .
- (c) the constant function  $x \mapsto 1$  on the set  $\{0, 1, 2\}$ .
- (d) the constant function  $x \mapsto 1$  on the set  $\{-2, -1, 0, 1, 2\}$ .
- (e) the function  $x \mapsto x^2$  on the set  $\{0, 1, 2\}$ .
- (f) the function  $x \mapsto x^2$  on the set  $\{-2, -1, 0, 1, 2\}$ .
- (g) the function  $x \mapsto x^3$  on the set  $\{0, 1, 2\}$ .
- (h) the function  $x \mapsto x^3$  on the set  $\{-2, -1, 0, 1, 2\}$ .

**1-2.** Suppose X is a random variable having the discrete uniform distribution on the sample space  $\{1, 2, 3, 4, 5, 6\}$ .

- (a) Determine  $\Pr(X < 4)$ .
- (b) Determine  $\Pr(X \le 4)$ .
- (c) Determine  $\Pr(6 < X < 10)$ .

**1-3.** Suppose X is a random variable having PMF

$$f(x) = \frac{x}{21}, \qquad x = 1, 2, 3, 4, 5, 6$$

- (a) Determine E(X).
- (b) Determine  $E(X^2)$ .
- (c) Determine  $E\{(X-3)^2\}$ .

**1-4.** Suppose X is a Ber(p) random variable.

- (a) Show that  $E(X^k) = p$  for all positive integers k.
- (b) Determine  $E\{(X-p)^2\}$ .
- (c) Determine  $E\{(X-p)^3\}$ .
- **1-5.** Determine the set of real numbers  $\theta$  such that

$$f_{\theta}(x) = \begin{cases} \theta, & x = x_1 \\ \theta^2, & x = x_2 \\ 1 - \theta - \theta^2, & x = x_3 \end{cases}$$

is a PMF on the sample space  $\{x_1, x_2, x_3\}$ .